

Programming as an Everyday Tool in Mathematical Education



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ICME-13, 2016
HAMBURG, GERMANY

Programming, Geometry, and Mathematics

- “Programs are more *discussable* than traditional mathematical activities: one can talk about their structure, one can talk about their development, their relation to one another, and to the original problem” [1]
- Tasking a student to write a program can be compared to giving a constructive proof [2]
- Describing a geometrical construction is nothing less than giving an appropriate algorithm for it [3]
- The final form of the description of a geometric construction is the algorithm, which then can be translated to a computer language [4]

constructive proof variables modularization
telling the machine how to do it
geometric construction exactness
problem solving rigorous thinking algorithms
functions

Polygons, Tessellations, Congruent Triangle Constructions – with SCRATCH

```

move 100 steps
turn 120 degrees
move 100 steps
turn 120 degrees
move 100 steps
turn 120 degrees
    
```

```

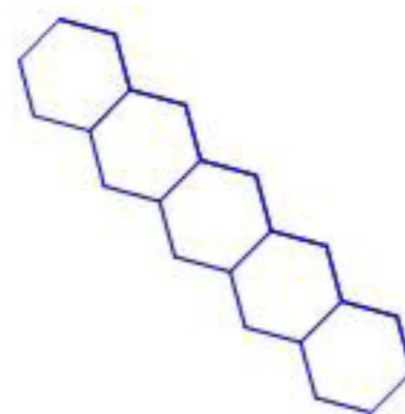
repeat 3
  move 100 steps
  turn 120 degrees
    
```

```

repeat 3
  move A steps
  turn 120 degrees
    
```

```

repeat 8
  repeat 3
    move A steps
    turn 120 degrees
  change A by 15
    
```



```

repeat 5
  repeat 6
    move 20 steps
    turn 60 degrees
  move 20 steps
  turn 60 degrees
  move 20 steps
  turn 300 degrees
  turn 240 degrees
  repeat 5
    move 20 steps
    turn 300 degrees
    move 20 steps
    turn 60 degrees
  turn 240 degrees
  move 20 steps
  turn 300 degrees
  move 20 steps
  turn 300 degrees
    
```

```

repeat 5
  repeat 5
    repeat 6
      move 20 steps
      turn 60 degrees
    move 20 steps
    turn 60 degrees
    move 20 steps
    turn 300 degrees
    turn 240 degrees
    repeat 5
      move 20 steps
      turn 300 degrees
      move 20 steps
      turn 60 degrees
    turn 240 degrees
    move 20 steps
    turn 300 degrees
    move 20 steps
    turn 300 degrees
    
```

```

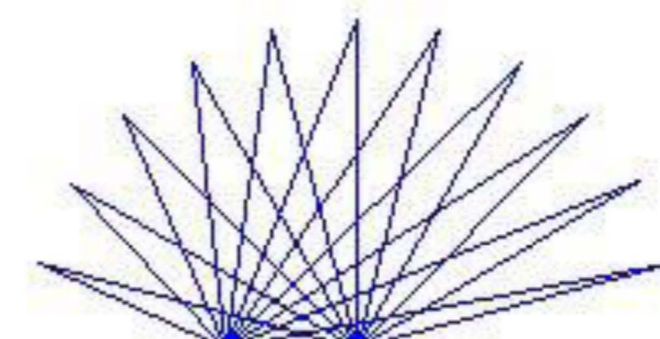
go to x: 0 y: 0
move 75 steps
turn 80 degrees
move 123 steps
go to x: 0 y: 0
    
```

```

go to x: 0 y: 0
move A steps
turn 180 - Beta degrees
move C steps
go to x: 0 y: 0
    
```

```

repeat 11
  move A steps
  turn 180 - Beta degrees
  move C steps
  go to x: 0 y: 0
  change Beta by 15
  point in direction 90
    
```



We see programming as an essential technique that should be treated just like any other mathematical tool
To be used when appropriate, not to be applied when other tools are more useful, and not taught for its own sake

References:

- [1] W. Feurzeig, S. Papert, M. Bloom, R. Grant, and C. Solomon. *Programming-languages as a conceptual framework for teaching mathematics*. SIGCUE Outlook, 4(2):13–17, Apr. 1970.
- [2] K. M. Strecker. *Informatics for all - how much programming is necessary?*. PhD thesis, University of Göttingen, 2009.
- [3] G. Holland. On the Relevance of Construction Exercises in the Geometry *Der Mathematikunterricht*, 20(1):71–86, 1974.
- [4] B. Schmidt-Thieme. *Explaining as a Competence in an Interdisciplinary Perspective*. In Beiträge zum Mathematikunterricht, Hildesheim, 2009. Franzbecker.